

## **Lecture/Laboratory #3**

### **Outline:**

1. Review RC, LC filters and some important points of previous lecture
2. Discuss some laboratory problems/works
3. Rectification
4. Ckts with bipolar transistors
  - Voltage amplifier
  - Voltage conversion
  - Transistor switch, current source
  - Common emitter ampl. And differ. Ampl.
5. **Laboratory works**
  - (a) Curve tracers for LC filters

## RC Differentiators

RC differentiator: the same circuit as high-pass filter. Such circuit can be considered as high-pass filter of differentiator depending on domain: frequency domain  $\Rightarrow$  filter, time domain  $\Rightarrow$  differentiator.

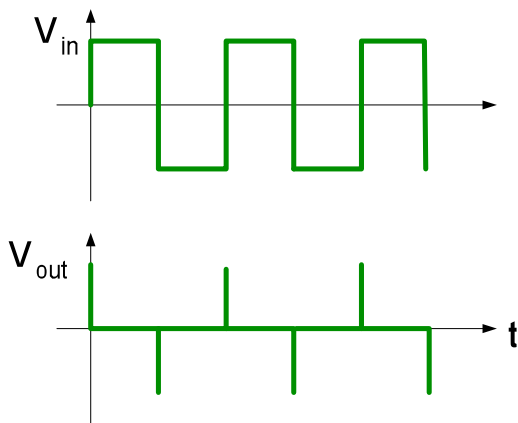
$$I = C \frac{d}{dt} (V_{in} - V_{out}) = V_{out} / R$$

$\uparrow$   
 Voltage across C

If R and C are small, such that  $dV_{out}/dt \ll dV_{in}/dt$ , then

$$C \frac{dV_{in}}{dt} \approx \frac{V_{out}}{R} \Rightarrow \underbrace{V_{out}(t) = RC \frac{dV_{in}(t)}{dt}}$$

Output  $\sim$  to the rate of change of input



Relation between high-pass filter and differentiator?

Differentiator:  $V_{out} \ll V_{in}$

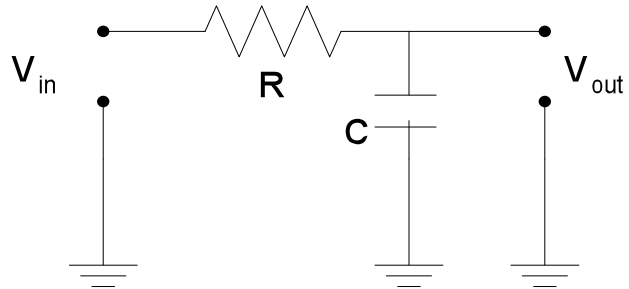
From frequency response of h - p filter  $\omega \ll \omega_{3dB} \Rightarrow$

$$\underline{\omega \ll \frac{1}{RC}} \quad \text{or} \quad \underline{R \ll \frac{1}{\omega C}}$$

## Low-pass Filters

By interchanging R and C in previous circuit we can get opposite frequency behavior in a RC filter.

$Z_{\text{tot}}$  for both ckts (high- and low-pass) is the same, hence:



$$V_{\text{out}} = V_{\text{in}} \frac{1/\omega C}{\left(R^2 + 1/\omega^2 C^2\right)^{1/2}} =$$

$$= V_{\text{in}} \left[ 1 + (2\pi\nu RC)^2 \right]^{-1/2}$$

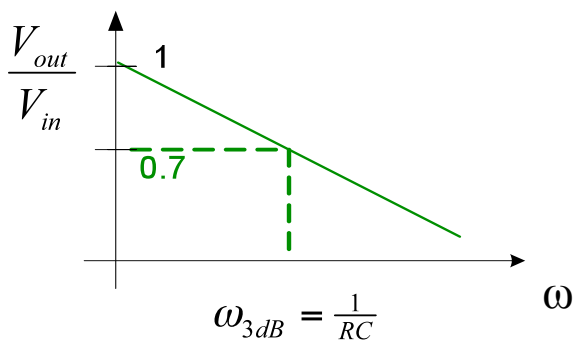
**Low-pass filter**  
(rejecting high  $\omega$ )

and

$$\omega_{3dB} = \frac{1}{RC}$$

For  $\omega < \omega_{3dB} \rightarrow$  **low-pass filter**

For  $\omega > \omega_{3dB} \rightarrow V_{\text{out}} / V_{\text{in}} \sim \omega^{-1}$



## Integrators

RC integrator: the same ckt as low-pass filter .

As in the case of high-pass filter/differentiator the integrator/low-pass filter ckt can be considered as low-pass filter in frequency domain or integrator in time domain.

In time domain voltage across  $R$  is  $V_{in} - V_{out}$  ,

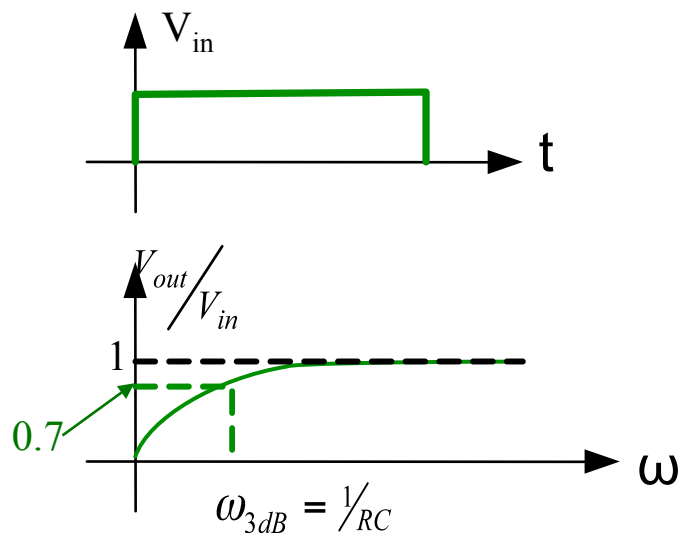
$$I = C \frac{dV_{out}}{dt} = \frac{V_{in} - V_{out}}{R}$$

For  $Z_R \gg Z_C$  (RC large)  $\Rightarrow V_{out} \ll V_{in}$  , hence

$$C \frac{dV_{out}}{dt} \approx \frac{V_{in}}{R} \Rightarrow V_{out}(t) = \underbrace{\frac{1}{RC} \int_0^t V_{in}(t) dt + const.}_{\text{Integrator, when } RC \gg 1/\omega}$$

$$\omega_{3dB} = \frac{1}{RC} ;$$

$$V_{3dB} = \frac{1}{2\pi RC}$$



## Integrators (cont.)

Inductor  $L$  in combination with  $R$  can also be used as low- and high-pass filters ( $RL$  – filters). However,  $RC$  filters are more convenient and less expensive to use.

## Resonant Circuits

“Active” filter  $\rightarrow$  combination of capacitor with inductor

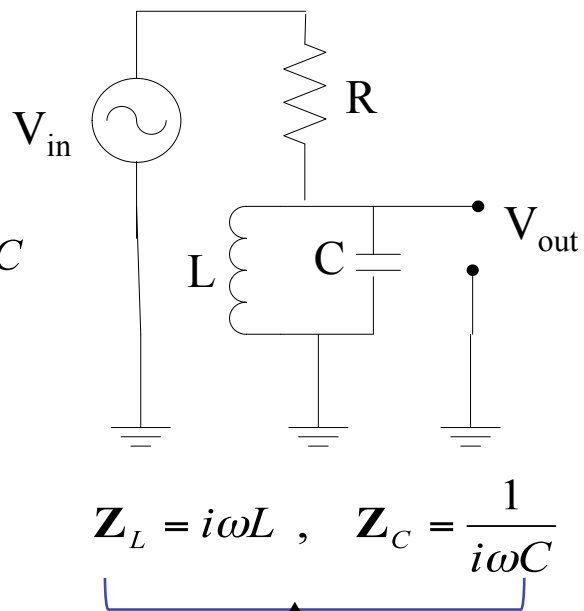
Parallel LC filter

$$\frac{1}{Z_{LC}} = \frac{1}{Z_L} + \frac{1}{Z_C} = \frac{1}{i\omega L} + i\omega C$$

$$Z_{LC} = \frac{i}{\frac{1}{\omega L} - \omega C}$$

for

$$\omega_0 = \frac{1}{\sqrt{LC}} \rightarrow Z_{LC} = \infty$$



$$Z_L = i\omega L, \quad Z_C = \frac{1}{i\omega C}$$

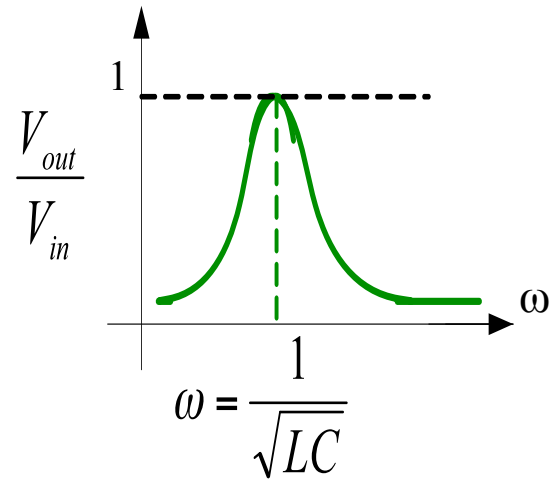
Divider with

$$V_{out} = V_{in} \frac{Z_{LC}}{Z_{LC} + R}$$

## Resonant Circuits (cont.)

for

$$Z_{LC} = \infty \Rightarrow V_{out}/V_{in} = 1$$

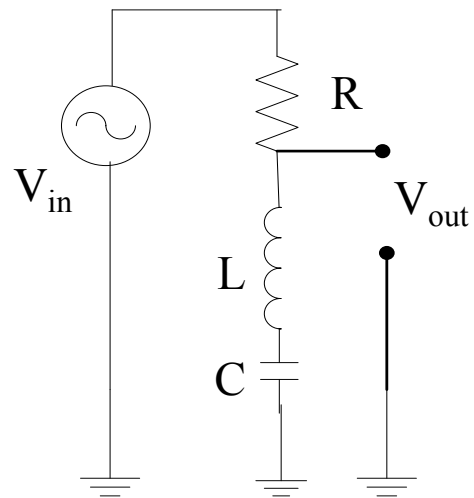
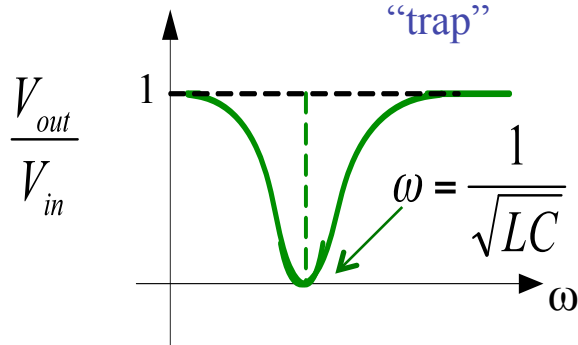


## Series LC filter

$$Z_{LC} = i\omega L + \frac{1}{i\omega C} = i\left(\omega L - \frac{1}{\omega C}\right)$$

For  $\omega_0 = \frac{1}{\sqrt{LC}} \Rightarrow Z_{LC} = 0$

$\Downarrow$   
 $\underline{V_{out} = 0}$   
 “trap”



At  $\omega_0$  signal short to ground

## In Laboratory:

Curve tracers for LC “active” filters

- (a) Parallel LC filter
- (b) Series LC filter

Look for resonances (Change L,C,R and observe how sharp resonances could be)

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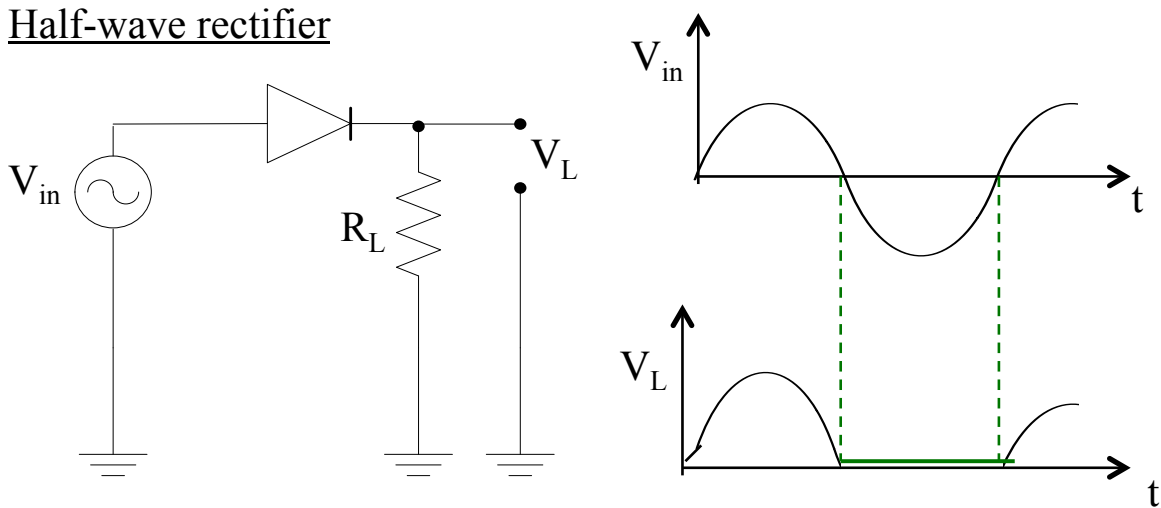
## Rectification

Rectifier changes AC current/voltage to DC. Diode play the most important role (it is most important function of diode)

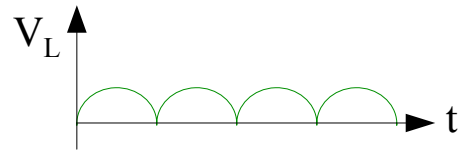
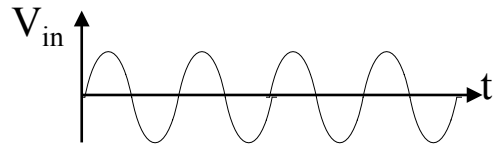
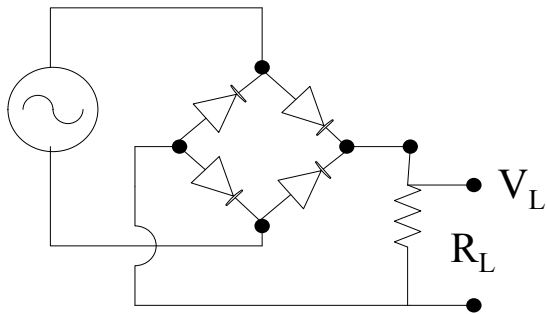
Two things about diodes:

- (a) Diode doesn't obey Ohm's law (diode doesn't have resistance in common sense)
- (b) Diode in ckt have no Thévenin's equivalent

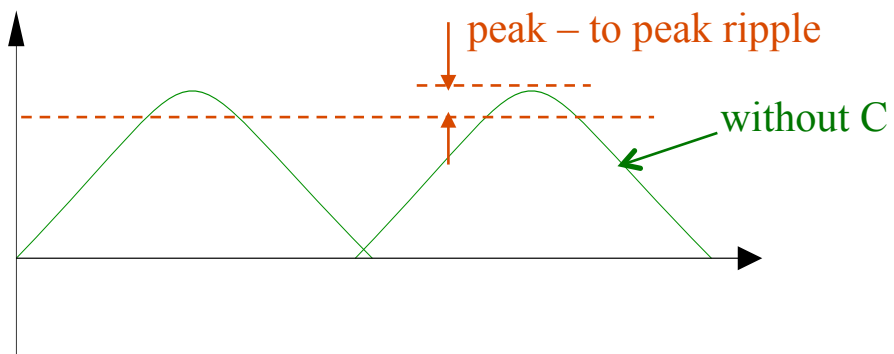
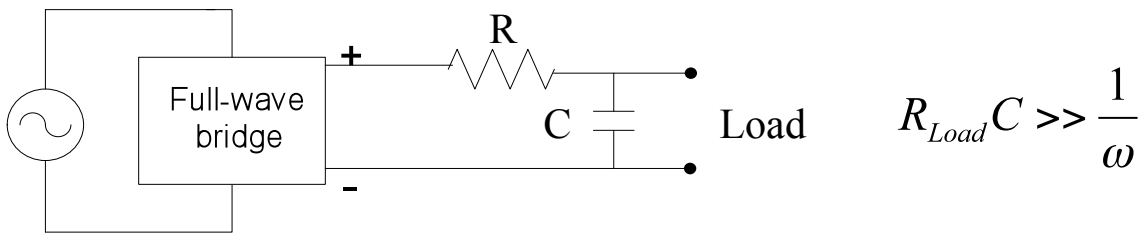
### Half-wave rectifier



## Full-wave bridge rectifier



## Filtering rectifier





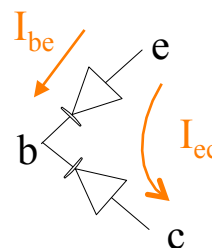
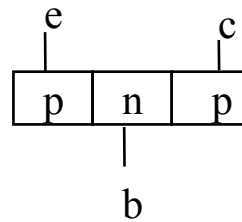
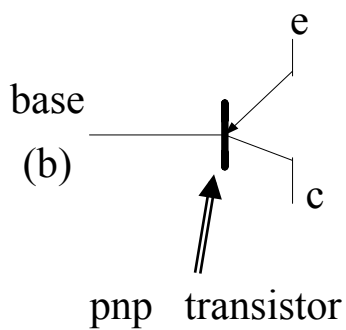
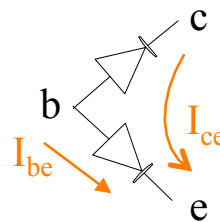
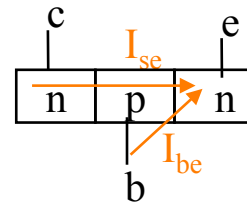
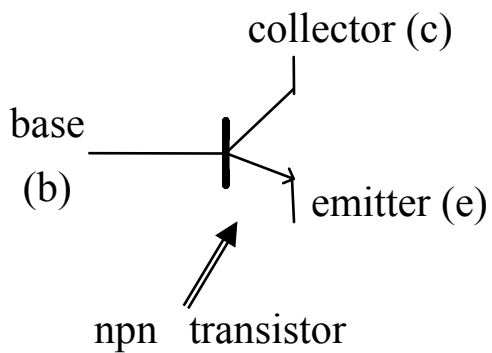
## Introduction to Transistors

Transistor : 3 – terminal device

Two types of transistors: **npn** and **pnp**

n – electron dominated

p – holes dominated



## Semiconductors as Diodes

Semiconductor materials ([Fig. A1](#))

- (a) Single species of atoms (silicon, Si; Germanium, Ge)  
([Table 1](#))
- (b) Composed materials (e.g. Gallium Arsenide, GaAs  $\Rightarrow$  III – V; Lead Sulfur, PbS  $\Rightarrow$  IV – VI) ([Table 2](#))

Importance of Si as a component (lower leakage than Ge ,  
abundance)

Energy Levels  $\Rightarrow$  Bands:

Valence Band,  $\Rightarrow$  Upper:  $E_v$

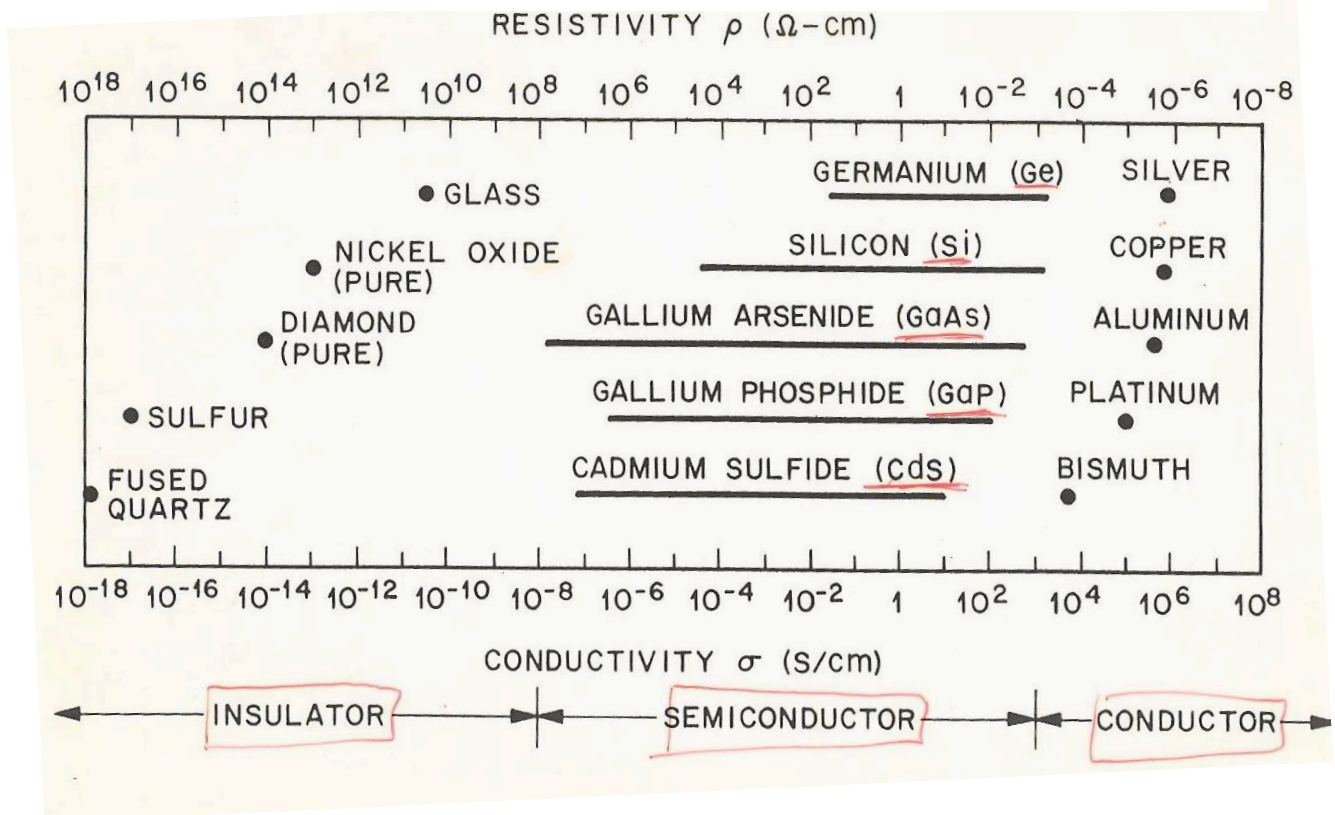
Conduction Band  $\Rightarrow$  Lower:  $E_c$

Bandgap,  $E_g$



Most important parameter in semiconductor Physics.

Fig. A1. Typical range of resistivity (conductivities) for insulators, semiconductors, and conductors



**Table 1** Portion of the Periodic Table Related to Semiconductors

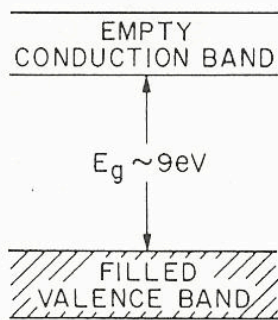
Period	Column II	III	IV	V	VI
2		B Boron	C Carbon	N Nitrogen	
3	Mg Magnesium	Al Aluminum	Si Silicon	P Phosphorus	S Sulfur
4	Zn Zinc	Ga Gallium	Ge Germanium	As Arsenic	Se Selenium
5	Cd Cadmium	In Indium	Sn Tin	Sb Antimony	Te Tellurium
6	Hg Mercury		Pb Lead		

**Table 2** Element and Compound Semiconductors

Element	IV-IV Compounds	III-V Compounds	II-VI Compounds	IV-VI Compounds
Si Ge	SiC	AlAs AlSb BN GaAs GaP GaSb InAs InP InSb	CdS CdSe CdTe ZnS ZnSe ZnTe	PbS PbTe

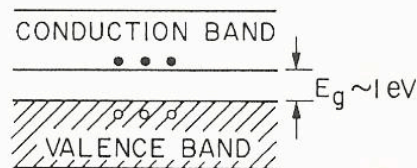
**Fig. A2**

Energy Bands (Schematic)



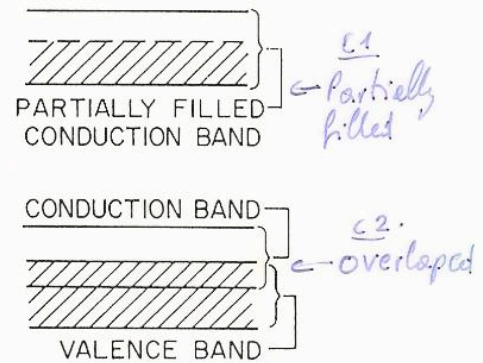
(a)

Insulators



(b)

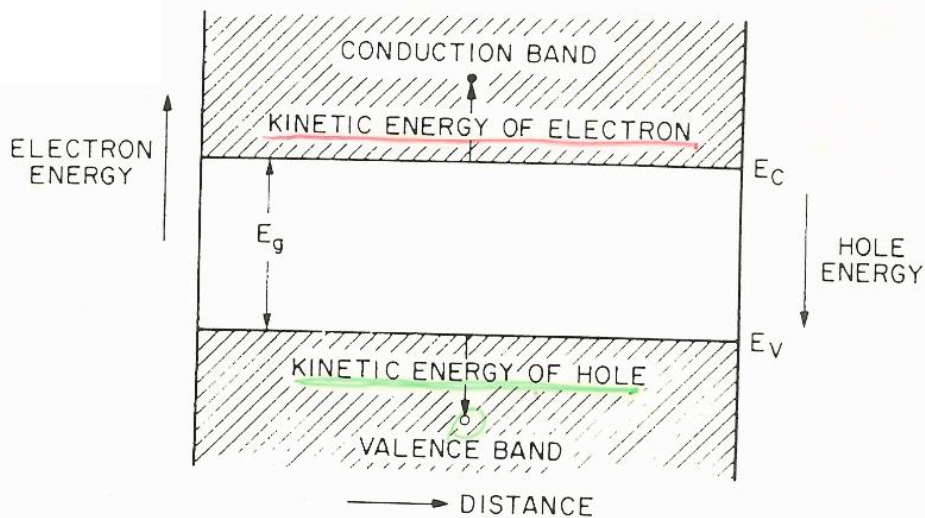
Semiconductors



(c)

Conductors

**Fig. A3**



Potential and kinetic energies in band representation

## Semiconductors as Diodes (cont.)

Isolators  $\Rightarrow$  Large bandgaps (e.g.  $\text{SiO}_2$  :  $E_g \sim 9 \text{ eV}$ )

$\Downarrow$   
Empty conduction band  $\Rightarrow$  no free electrons to carry current

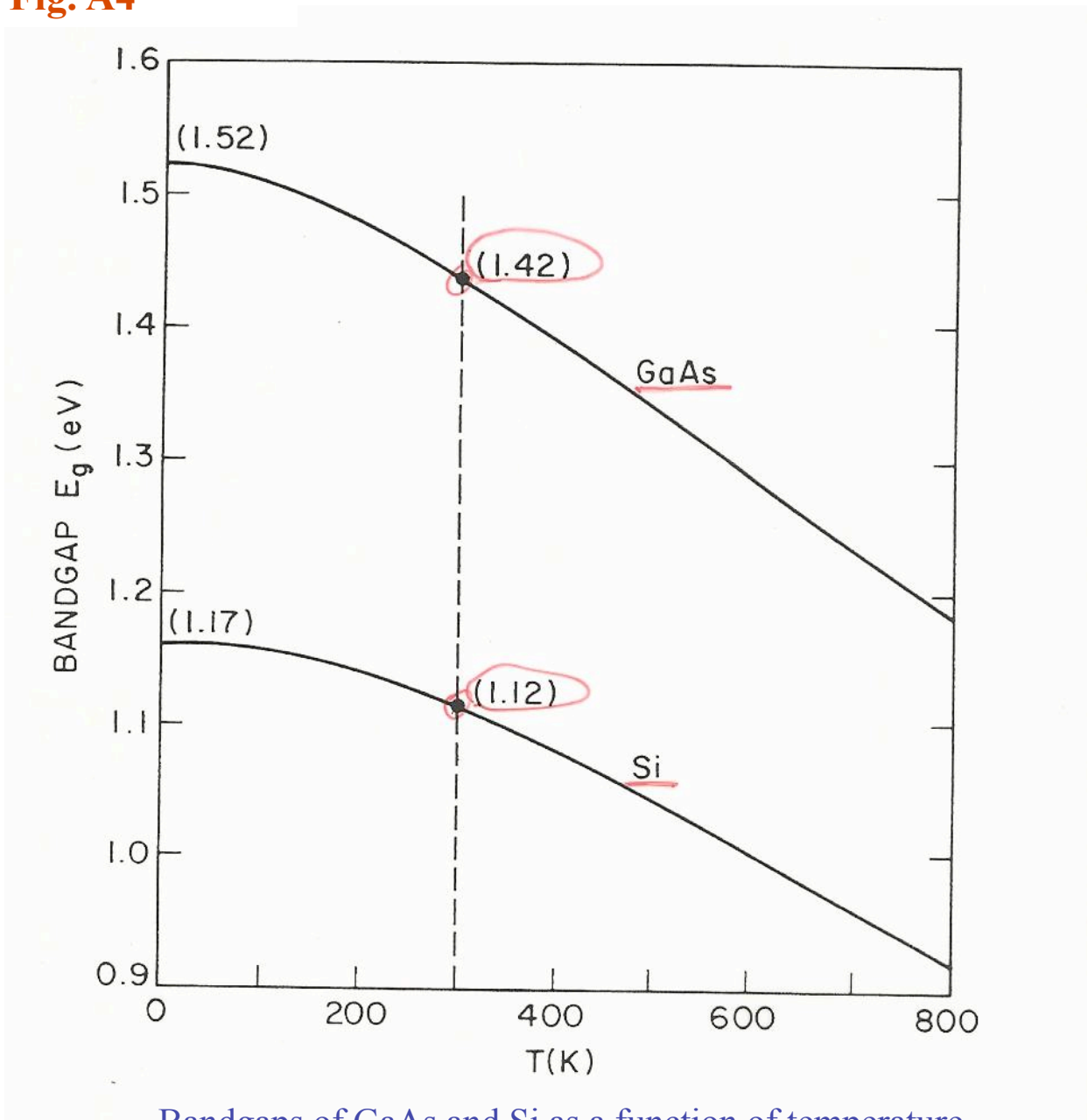
Semiconductors  $\Rightarrow$  Moderate bandgaps (e.g. Si :  $E_g \sim 1.1 \text{ eV}$   
e.g. GaAs:  $E_g \sim 1.4 \text{ eV}$ )

$\Downarrow$   
Thermal energy (thermal vibrations) may move electrons to conduction band  $\Rightarrow$  can move under E – field  $\Rightarrow$  current  
[minus electrons in valence band (holes)]

Conductors  $\Rightarrow$  (1) Conduction band is partially filled

$\swarrow$  [ (2) Conduction and valence bands are overlapped  $\Rightarrow$  no bandgap  
current can rapidly occur

**Fig. A4**

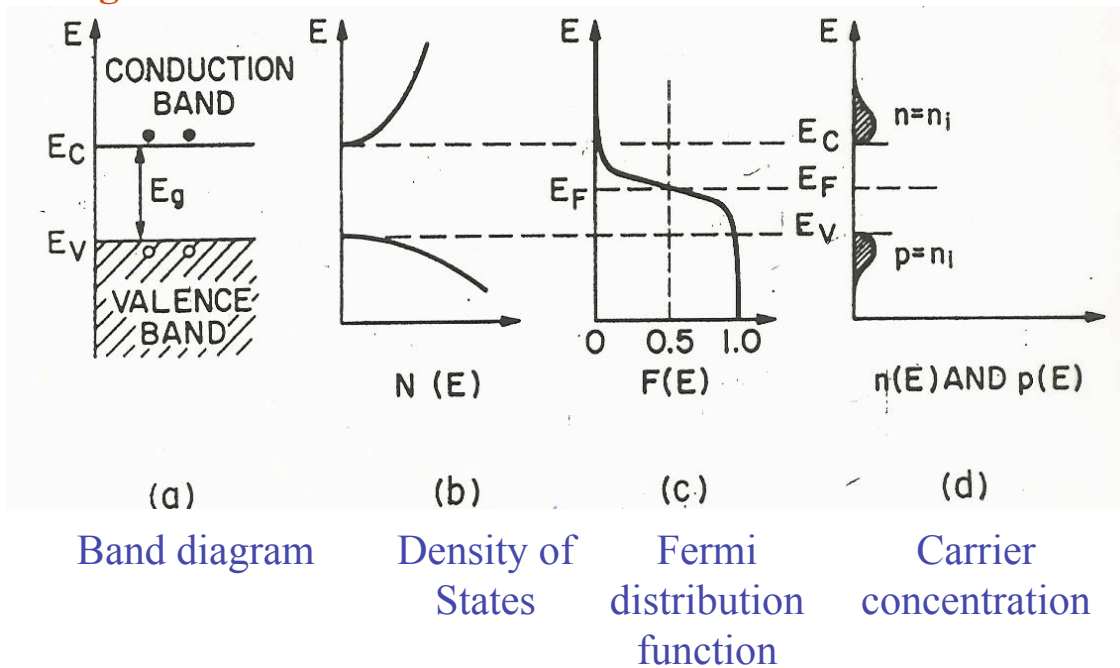


Bandgaps of GaAs and Si as a function of temperature

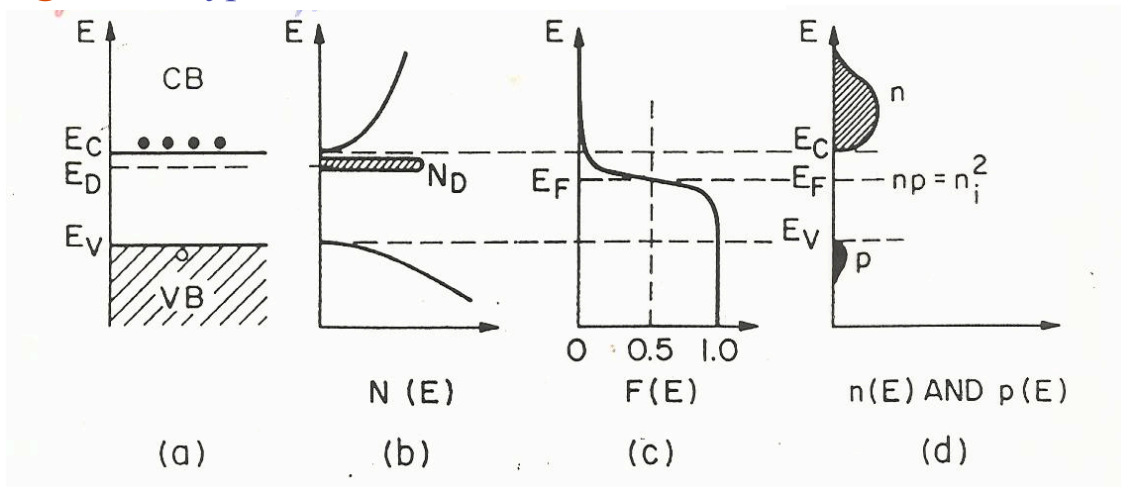


## Intrinsic and n – type Semiconductors (or p – type)

**Fig. A5.** Intrinsic Semiconductor



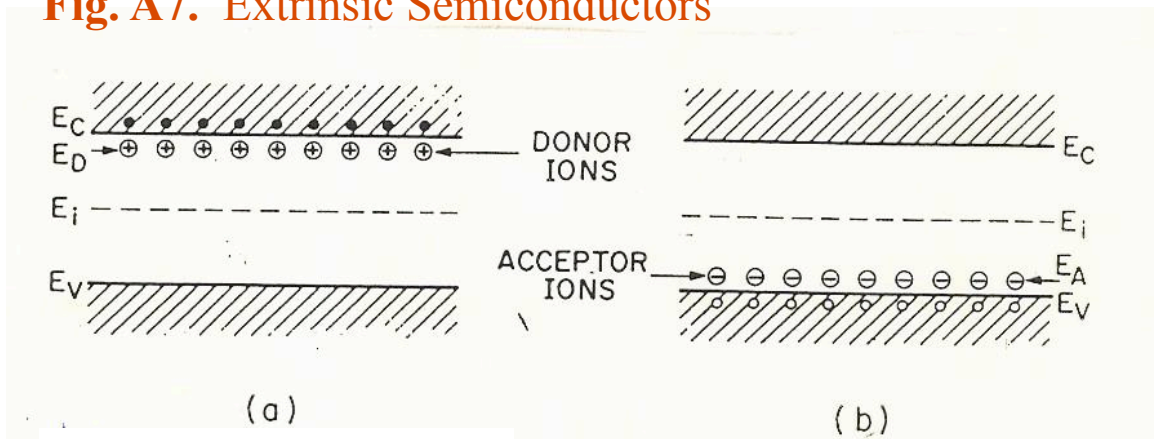
**Fig. A6.** n-type Semiconductors



$$F(E) = \frac{1}{1 + e^{(E-E_F)/kT}} \Rightarrow \begin{cases} F(E) \approx e^{-(E-E_F)/kT} & E - E_F \geq 3kT \\ F(E) \approx 1 - e^{-(E_F-E)/kT} & E - E_F \leq 3kT \end{cases}$$



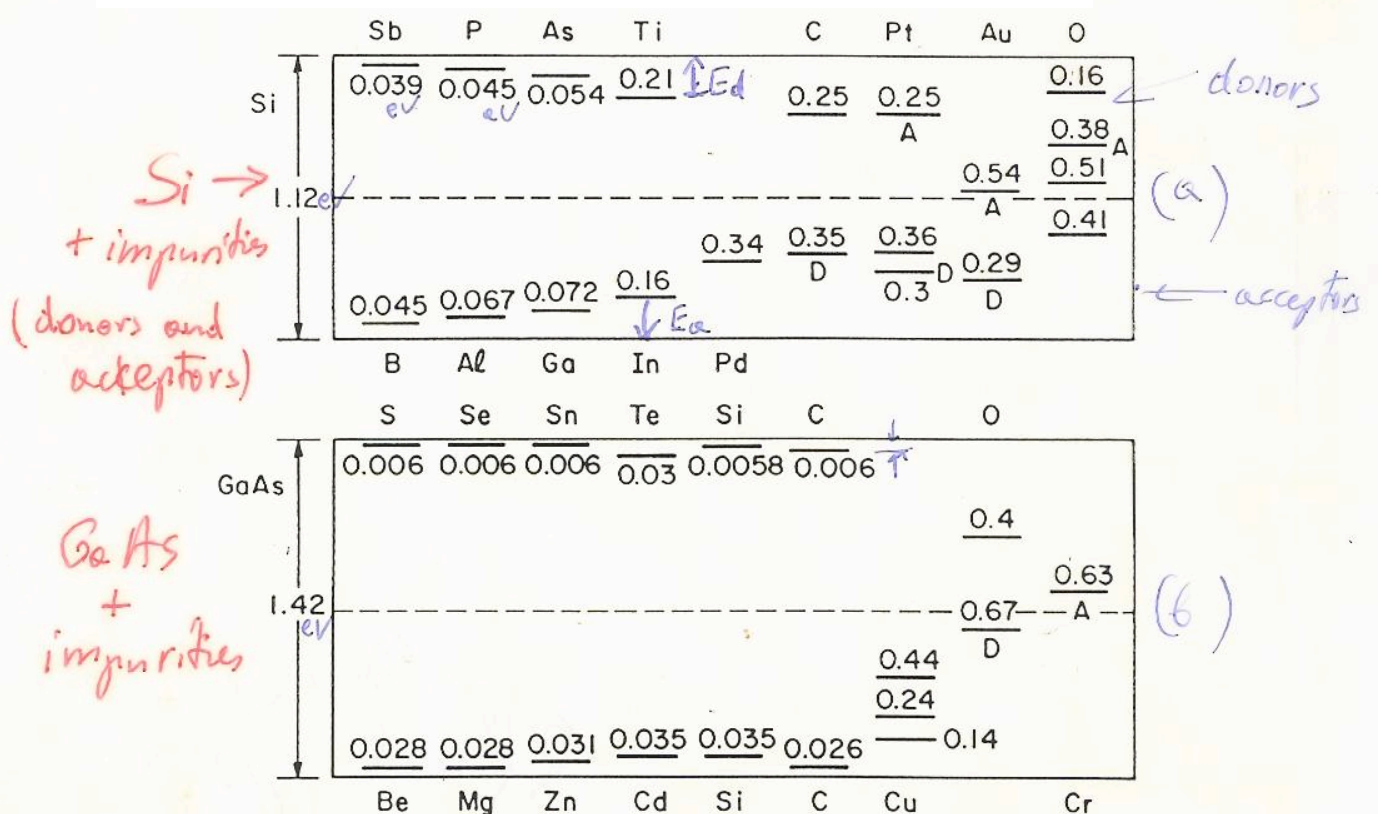
**Fig. A7. Extrinsic Semiconductors**



With donor ions

With acceptor ions

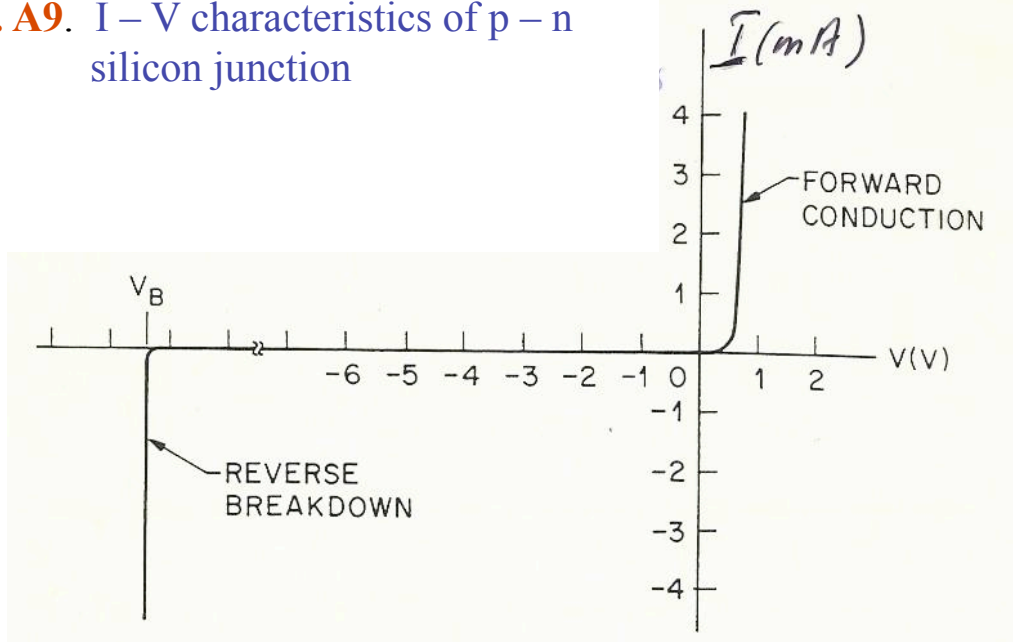
**Fig. A8**



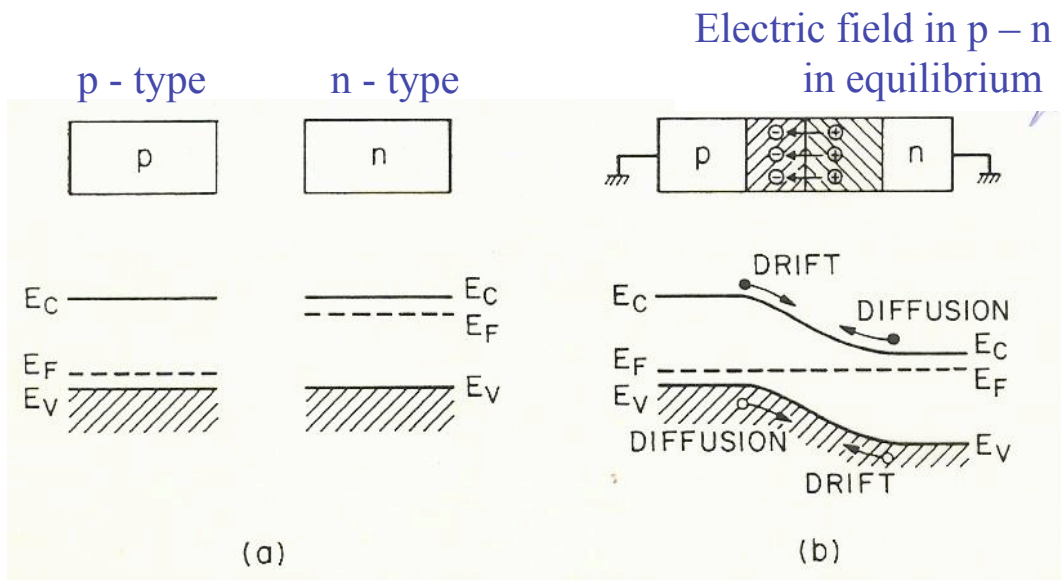
Ionization energies in Si (a) and GaAs (b) for different impurities

## Diodes (p – n junction)

**Fig. A9.** I – V characteristics of p – n silicon junction

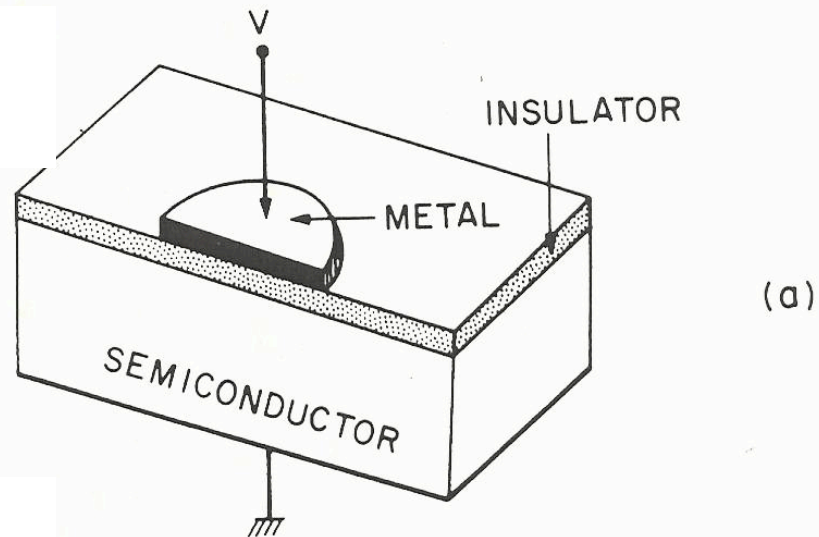


**Fig. A10.** Doped semiconductors and p – n junction

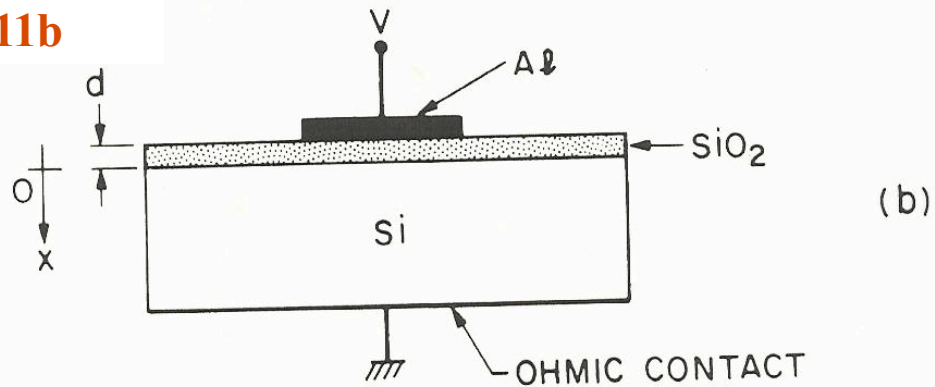


## The MOS Diode

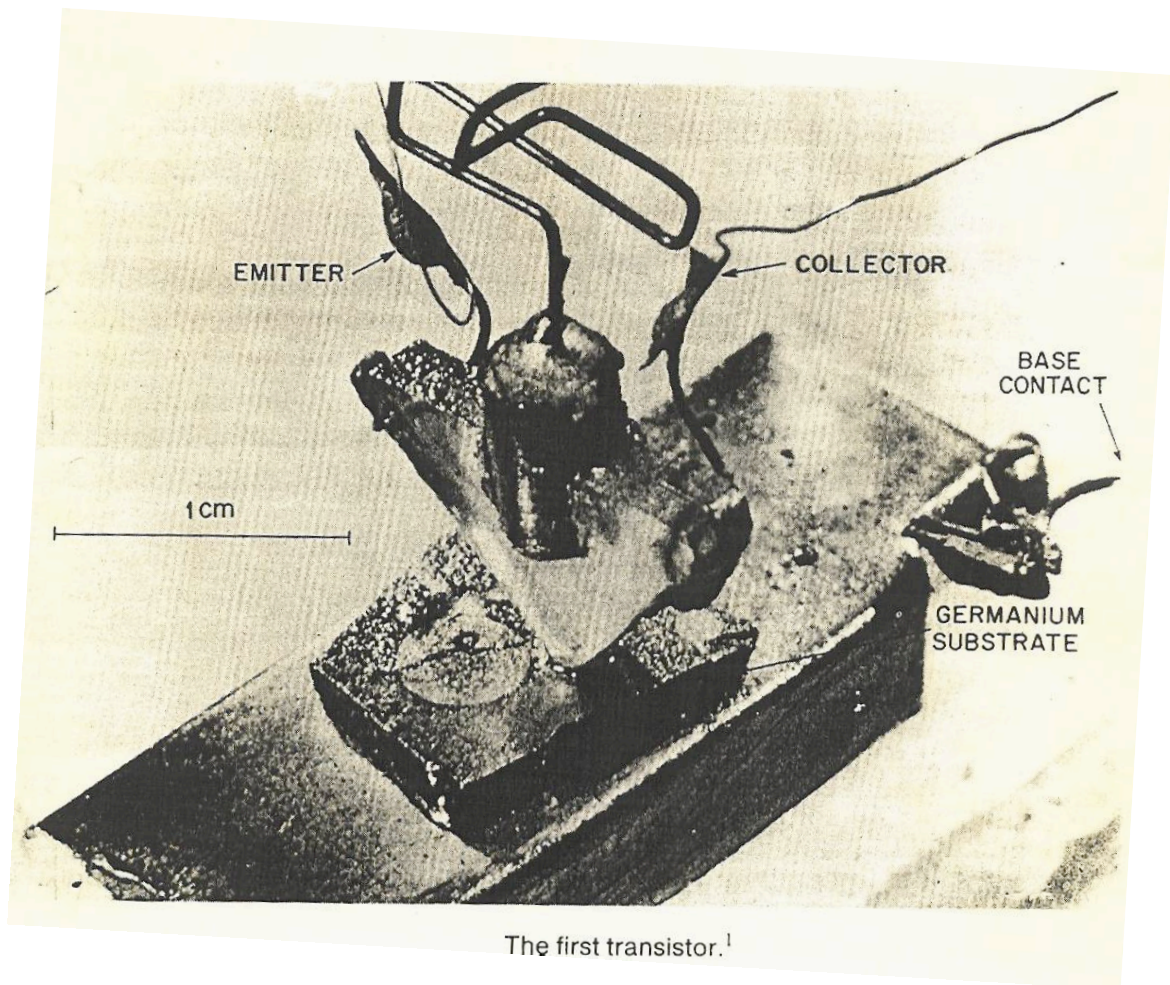
**Fig. A11a**



**Fig. A11b**



(a) Perspective view of an MOS diode. (b) Cross section of an MOS diode



The first transistor.<sup>1</sup>